

Happy Tuesday, February 28th

Prove:

$$2(3x^3 - 21x^2 + 12x) = 3x(x-4)(x-3) \quad \text{RHS}$$

$$3x(x^2 - 7x + 12) \quad \text{FOIL}$$

$$\text{LHS} \neq (3x^3 - 21x^2 + 36x) \quad \square$$



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Proofs are like sandwiches... $\boxed{\tan x + \cot x} = \underline{\sec x \csc x}$



You know what's on top

...And what's on bottom

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Our Ingredients for Trig Proofs



The meat: ALGEBRA

The Veggies: Definitions



The Sauces:
Explanations

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The meat: ALGEBRA

Factoring

Adding/Subtracting Fractions

Distributing

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The Veggies: Definitions/Identities

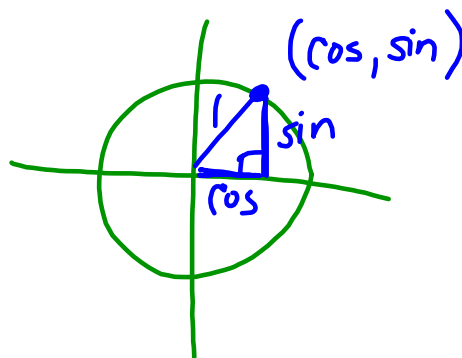
$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\csc \theta = \frac{1}{\sin \theta}$$

$$\sec \theta = \frac{1}{\cos \theta}$$

$$\cot \theta = \frac{1}{\tan \theta} = \frac{\cos \theta}{\sin \theta}$$



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$$\frac{\sin^2 \theta}{\cancel{\sin^2 \theta}} + \frac{\cos^2 \theta}{\cancel{\cos^2 \theta}} = 1$$

divide by
 $\sin^2 \theta$

 \Rightarrow

$$1 + \cot^2 \theta = \csc^2 \theta$$

divide by
 $\cos^2 \theta$

 \Rightarrow

$$\tan^2 \theta + 1 = \sec^2 \theta$$

Feb 28-9:02 AM

The Sauces: Explanations

Will not be required on the test, but will be required on homework.

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LHS

$$\tan x + \cot x = \sec x \cdot \csc x$$

By def
 $\frac{\sin x}{\cos x} + \frac{\cos x}{\sin x}$

Common denom.
 $\frac{\sin x \cdot \sin x}{\sin x \cdot \cos x} + \frac{\cos x \cdot \cos x}{\sin x \cdot \cos x}$

Add Fractions
 $\frac{(\sin^2 x + \cos^2 x)}{\sin x \cos x}$

Pythagorean identity
 $\frac{1}{\sin x \cdot \cos x}$

Split fraction
 $\frac{1}{\sin x} \cdot \frac{1}{\cos x}$

$\csc x \cdot \sec x$

$\sec x \cdot \csc x = \boxed{\sec x \csc x}$

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$$(\sin x)(\cot x + \cos x \tan x) = \cos x + \sin^2 x$$

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