

Properties of Logarithms

Expand each logarithm.

1) $\log(6 \cdot 11)$

$$\log 6 + \log 11$$

3) $\log\left(\frac{6}{11}\right)^5$

$$5 \log\left(\frac{6}{11}\right)$$

$$5(\log 6 - \log 11)$$

5) $\log \frac{2^4}{5}$

$$\log 2^4 - \log 5$$

$$4 \log 2 - \log 5$$

7) $\log \frac{x}{y^6}$

$$\log x - \log y^6$$

$$\log x - 6 \log y$$

9) $\log \frac{u^4}{v}$

$$\log u^4 - \log v$$

$$4 \log u - \log v$$

11) $\log \sqrt[3]{x \cdot y \cdot z}$

$$\log (x \cdot y \cdot z)^{\frac{1}{3}}$$

$$\frac{1}{3} \log x \cdot y \cdot z$$

$$\frac{1}{3} (\log x + \log y + \log z)$$

2) $\log(5 \cdot 3)$

$$\log 5 + \log 3$$

4) $\log(3 \cdot 2^3)$

$$\log 3 + \log 2^3$$

$$\log 3 + 3 \log 2$$

6) $\log\left(\frac{6}{5}\right)^6$

$$6 \log \frac{6}{5}$$

$$6(\log 6 - \log 5)$$

8) $\log(a \cdot b)^2$

$$2 \log(ab)$$

$$2(\log a + \log b)$$

10) $\log \frac{x}{y^5}$

$$\log x - \log y^5$$

$$\log x - 5 \log y$$

12) $\log(x \cdot y \cdot z^2)$

$$\log x + \log y + \log z^2$$

$$\log x + \log y + 2 \log z$$

Condense each expression to a single logarithm.

13) $\log 3 - \log 8$

$$\log\left(\frac{3}{8}\right)$$

14) $\frac{\log 6}{3}$

$$\frac{1}{3} \log 6$$

$$\boxed{\log 6^{\frac{1}{3}}} \text{ or } \boxed{\log \sqrt[3]{6}}$$

15) $4\log 3 - 4\log 8$

$$\log 3^4 - \log 8^4$$

$$\boxed{\log\left(\frac{3}{8}\right)^4}$$

16) $\log 2 + \log 11 + \log 7$

$$\log(2 \cdot 11 \cdot 7)$$

$$\boxed{\log(154)}$$

17) $\log 7 - 2\log 12$

$$\log 7 - \log 12^2$$

either is OK

$$\boxed{\log \frac{7}{12^2}} = \boxed{\log \frac{7}{144}}$$

18) $\frac{2\log 7}{3}$

$$\frac{2}{3} \log 7$$

$$\boxed{\log 7^{\frac{2}{3}}} \text{ or } \boxed{\log \sqrt[3]{7^2}}$$

19) $6\log_3 u + 6\log_3 v$

$$\log_3 u^6 + \log_3 v^6 = \boxed{\log_3 u^6 v^6}$$

20) $\ln x - 4\ln y$

$$\ln x - \ln y^4 = \boxed{\ln \frac{x}{y^4}}$$

21) $\log_4 u - 6\log_4 v$

$$\log_4 u - \log_4 v^6 = \boxed{\log_4 \frac{u}{v^6}}$$

22) $\log_3 u - 5\log_3 v$

$$\log_3 u^3 - \log_3 v^5 = \boxed{\log_3 \frac{u^3}{v^5}}$$

23) $20\log_6 u + 5\log_6 v$

$$\log_6 u^{20} + \log_6 v^5 = \boxed{\log_6 \frac{u^{20}}{v^5}}$$

24) $4\log_3 u - 20\log_3 v$

$$\log_3 u^4 - \log_3 v^{20}$$

$$\boxed{\log_3 \frac{u^4}{v^{20}}}$$

Critical thinking questions:

25) $2(\log 2x - \log y) - (\log 3 + 2\log 5)$

$$2\left(\log \frac{2x}{y}\right) - \log(3 \cdot 5^2)$$

$$\log\left(\frac{2x}{y}\right)^2 - \log 75$$

$$\Rightarrow \boxed{\log \frac{4x^2}{75y}}$$

26) $\log x \cdot \log 2$